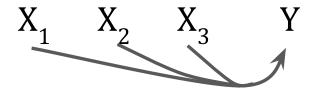
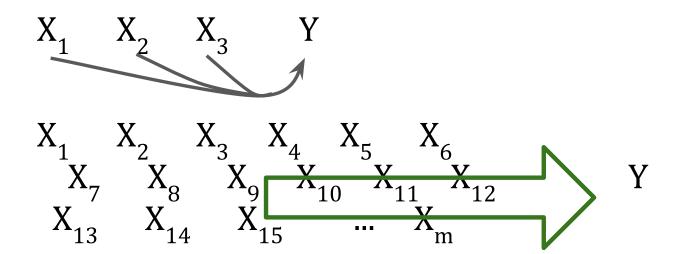
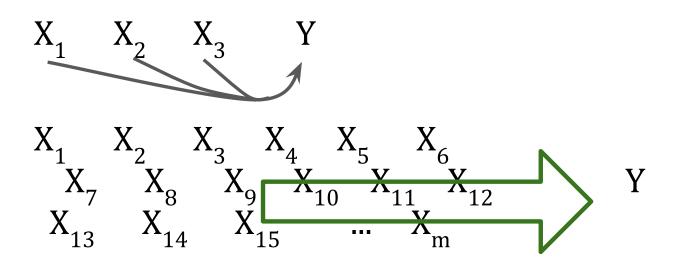
Large-Scale, Distributed Machine Learning

CSE545 - Spring 2020 Stony Brook University

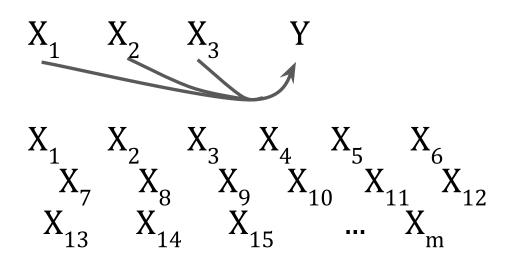
H. Andrew Schwartz

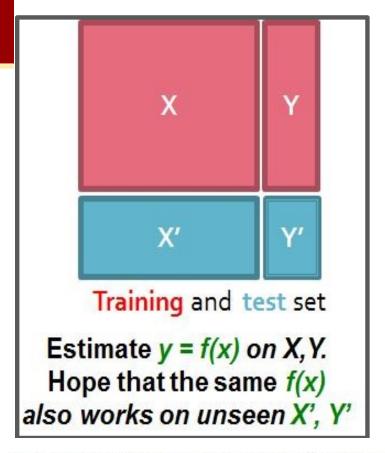






Task: Determine a function, f (or parameters to a function) such that f(X) = Y

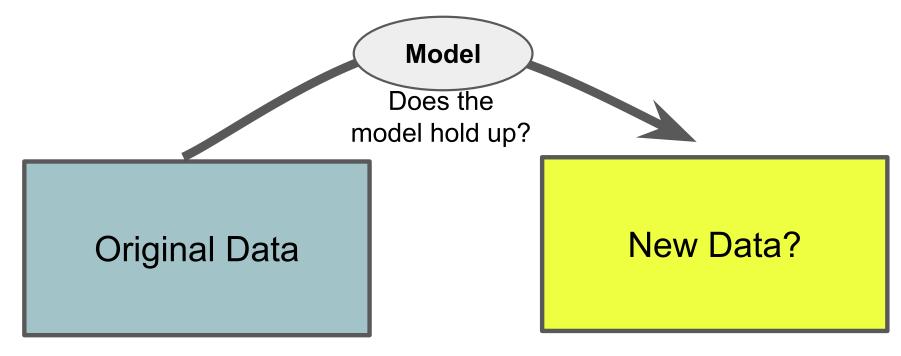




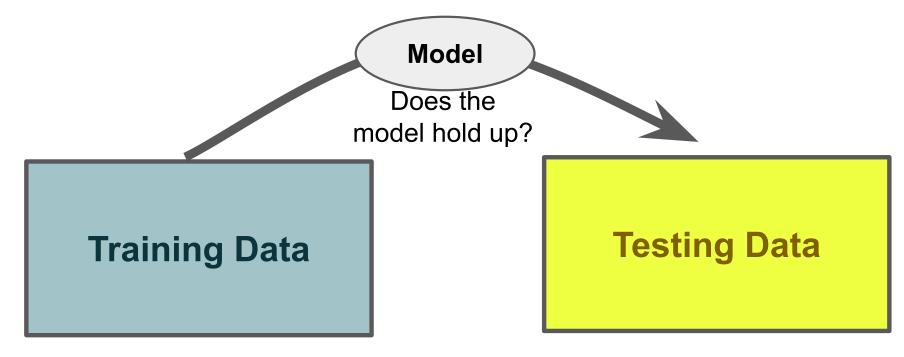
J. Leskovec, A. Rajaraman, J. Ullman: Mining of Massive Datasets, http://www.mmds.org

Task: Determine a function, f (or parameters to a function) such that f(X) = Y

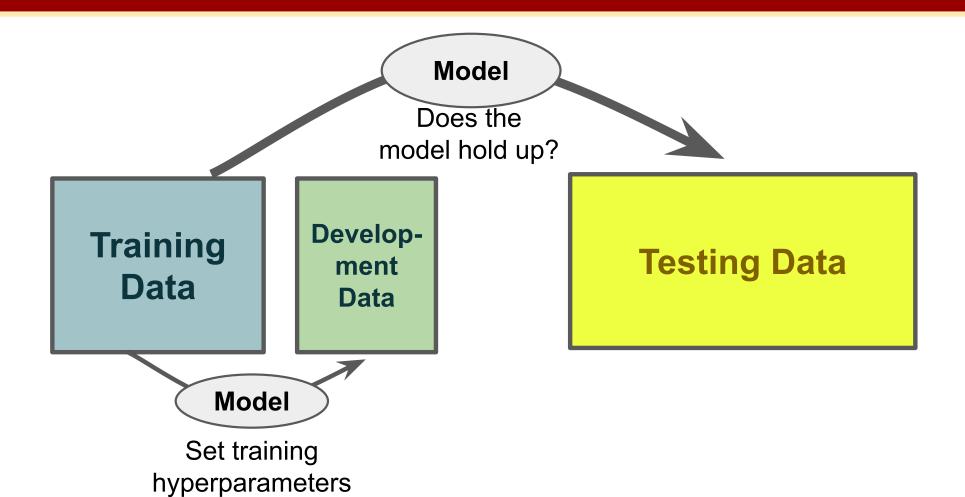
Common Goal: Generalize to new data



Common Goal: Generalize to new data

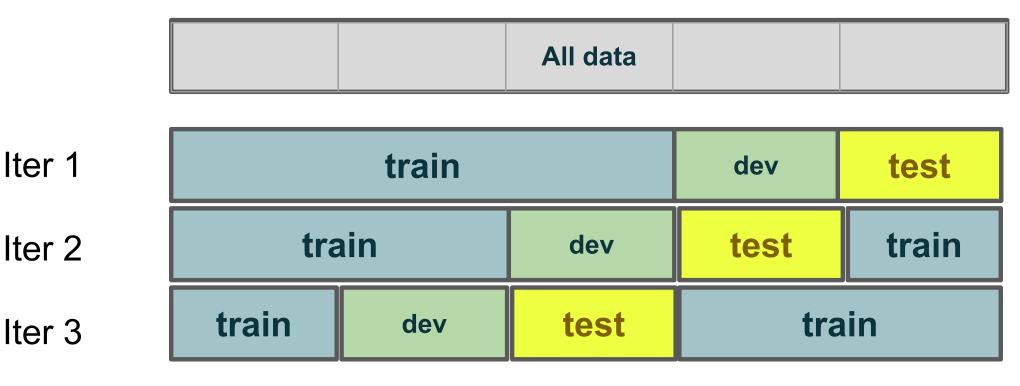


ML: GOAL



N-Fold Cross Validation

Goal: Decent estimate of model accuracy



Iter 1

Review: Distributed ML

Done very often in practice. Not talked about much because it's mostly as easy as it sounds.

- 1. Distribute copies of entire dataset
 - a. Train over all with different parameters
 - b. Train different folds per worker node.

Pro: Easy; Good for compute-bound; Con: Requires data fit in worker memories

2. Distribute data

- a. Each node finds parameters for subset of data
- b. Needs mechanism for updating parameters i Data Parellelism ver
 - ii. Distributed All-Reduce

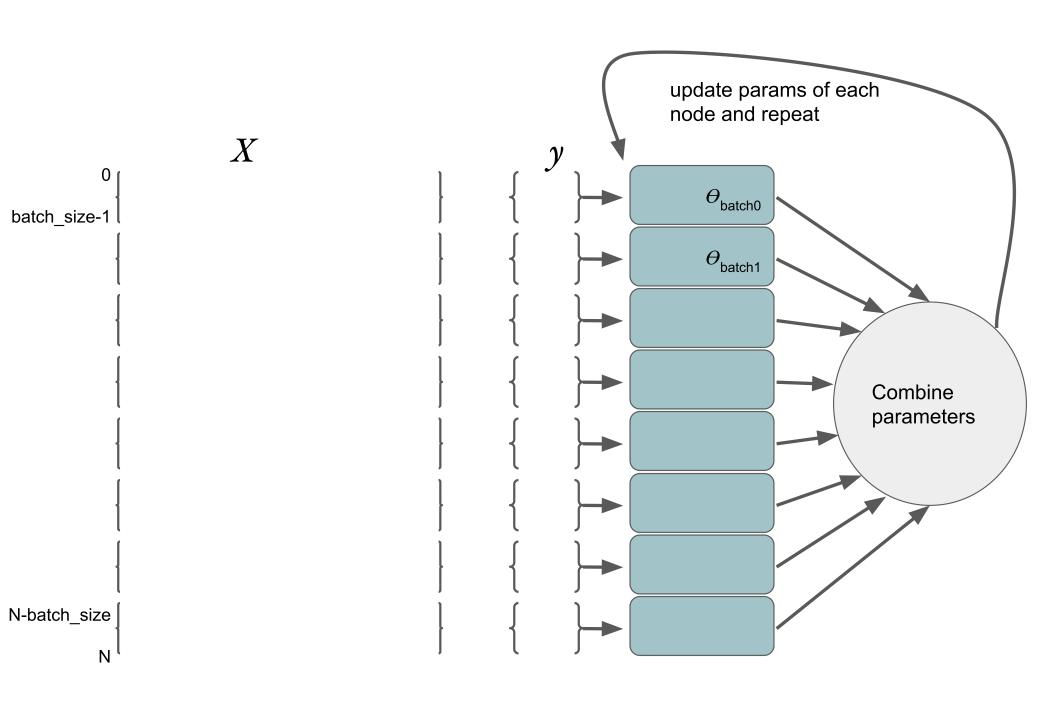
Preferred method for big data or very complex models (i.e. models with many internal parameters).

Pro: Flexible to all situations; Con: Optimizing for subset is suboptimal

3. Distribute model or individual operations (e.g. matrix multiply)

Pro: PaModel Parellelismed

Con: High communication for transferring Intermediar data.



- Linear modeling (linear and logistic regression)
- 2. Recurrent Neural Networks
 Where X is a sequence of data
- 3. Convolutional Neural Networks
 Where X might have spatial relationships

From Linear Models to Neural Nets

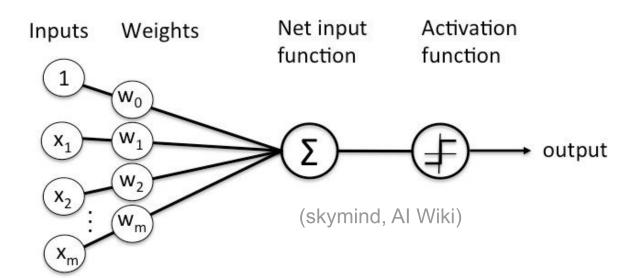
Linear Regression: y = wX

Neural Network Nodes: output = f(wX)

From Linear Models to Neural Nets

Linear Regression: y = wX

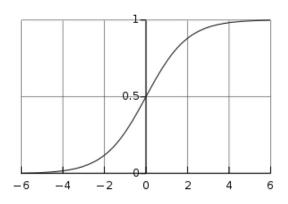
Neural Network Nodes: output = f(wX)



Common Activation Functions

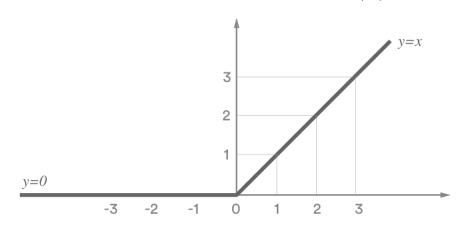
$$z = wX$$

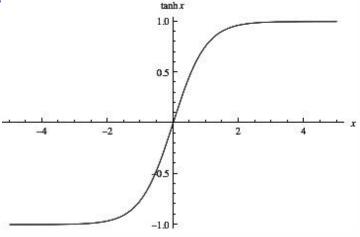
Logistic: $\sigma(z) = 1/(1 + e^{-z})$



Hyperbolic tangent: $tanh(z) = 2\sigma(2z) - 1 = (e^{2z} - 1)/(e^{2z} + 1)$

Rectified linear unit (ReLU): ReLU(z) = max(0, z)

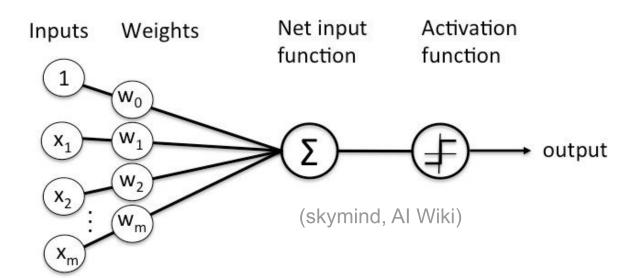




From Linear Models to Neural Nets

Linear Regression: y = wX

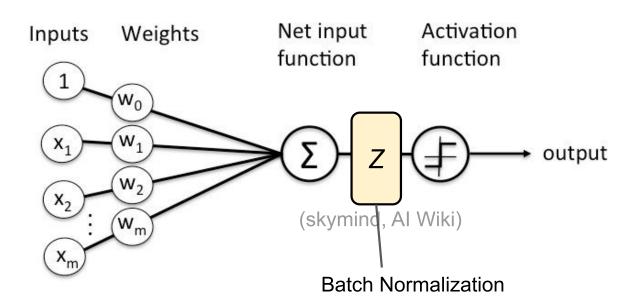
Neural Network Nodes: output = f(wX)



From Linear Models to Neural Nets

Linear Regression: y = wX

Neural Network Nodes: output = f(wX)



```
Input: Values of x over a mini-batch: \mathcal{B} = \{x_{1...m}\};

Parameters to be learned: \gamma, \beta

Output: \{y_i = \mathrm{BN}_{\gamma,\beta}(x_i)\}

\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^m x_i \qquad \text{// mini-batch mean}
\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2 \qquad \text{// mini-batch variance}
\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}} \qquad \text{// normalize}
y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv \mathrm{BN}_{\gamma,\beta}(x_i) \qquad \text{// scale and shift}
```

(loffe and Szegedy, 2015)

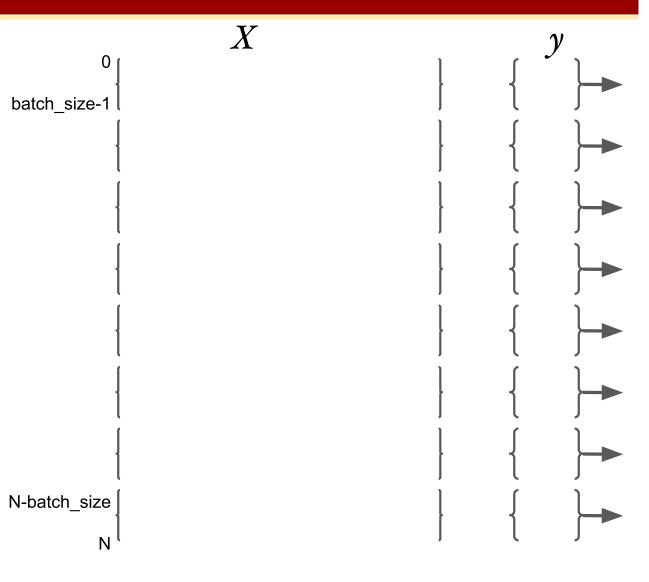
This is just standardizing! (but within the current batch of observations)

```
Input: Values of x over a mini-batch: \mathcal{B} = \{x_{1...m}\}; Parameters to be learned: \gamma, \beta

Output: \{y_i = \mathrm{BN}_{\gamma,\beta}(x_i)\}

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```

(loffe and Szegedy, 2015)



(but within the current batch of observations)

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$;

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$$\{y_i = BN_{\gamma,\beta}(x_i)\}$$

$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$$
 // mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$
 // mini-batch variance

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 // normalize

$$y_i \leftarrow \gamma \widehat{x}_i + \beta \equiv BN_{\gamma,\beta}(x_i)$$
 // scale and shift

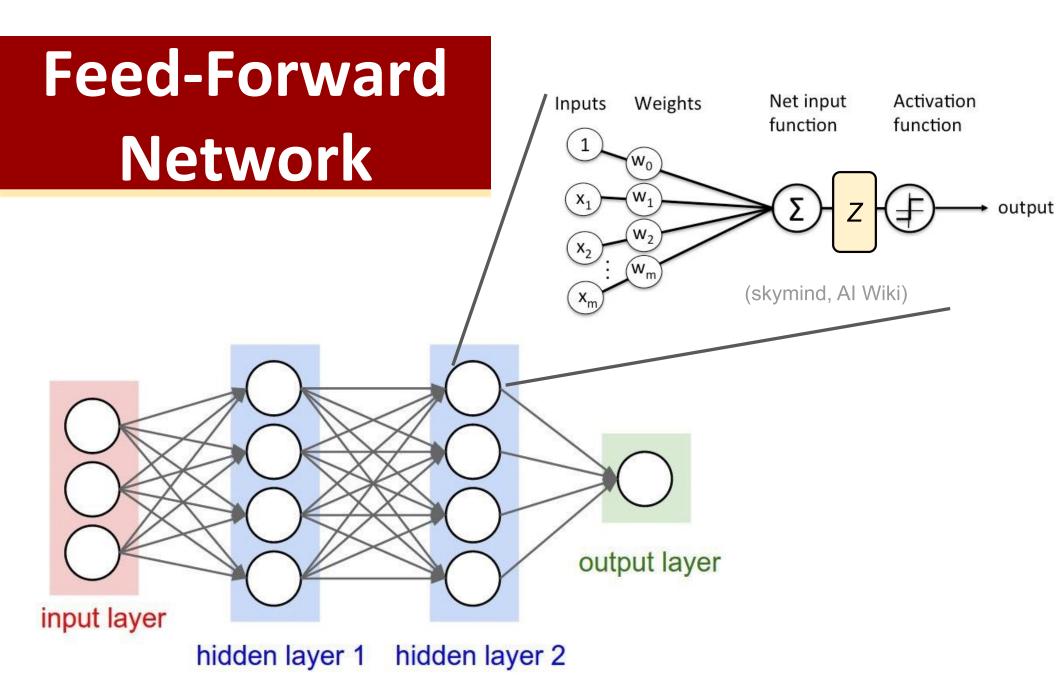
(loffe and Szegedy, 2015)

Why?

Empirically, it works!

This is just standardizing!

- Conceptually, generally good for weight optimization to keep data within a reasonable range (dividing by sigma) and such that positive weights move it up and negative down (centering).
- Small effect: When done over mini-batches, adds regularization due to differences between batches.



Recurrent Neural Network

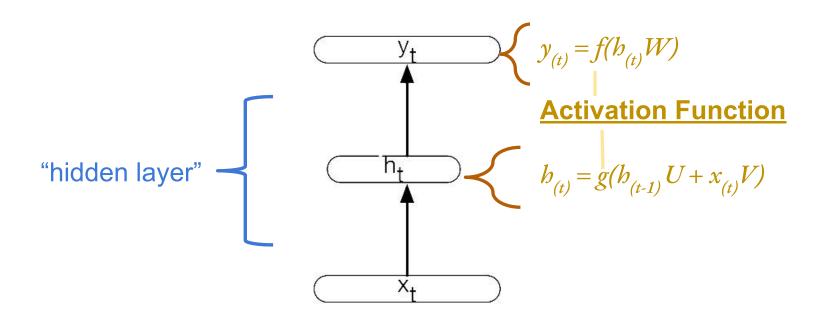


Figure 9.2 Simple recurrent neural network after Elman (Elman, 1990). The hidden layer includes a recurrent connection as part of its input. That is, the activation value of the hidden layer depends on the current input as well as the activation value of the hidden layer from the previous timestep.

(Jurafsky, 2019)

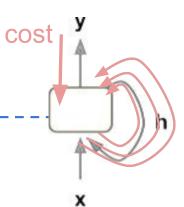
RNN: Optimization

cost

Backward Propagation through Time

```
#define forward pass graph:
h<sub>(0)</sub> = 0
for i in range(1, len(x)):
    h<sub>(i)</sub> = tf.tanh(tf.matmul(U,h<sub>(i-1)</sub>)+ tf.matmul(W,x<sub>(i)</sub>)) #update hidden
state
    y<sub>(i)</sub> = tf.softmax(tf.matmul(V, h<sub>(i)</sub>)) #update output
...
cost = tf.reduce_mean(-tf.reduce_sum(y*tf.log(y_pred))
```

RNN: Optimization



Backward Propagation through Time

```
#define forward pass graph:
h<sub>(0)</sub> = 0
for i in range(1, len(x)):
    h<sub>(i)</sub> = tf.tanh(tf.matmul(U, state
    y<sub>(i)</sub> = tf.softmax(tf.matmul
```

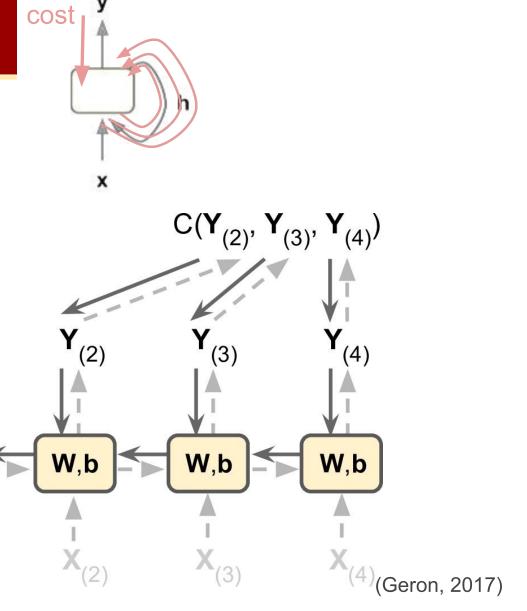
cost = tf.reduce_mean(-tf.redu

To find the gradient for the overall graph, we use **back propogation**, which *essentially* chains together the gradients for each node (function) in the graph.

With many recursions, the gradients can vanish or explode (become too large or small for floating point operations).

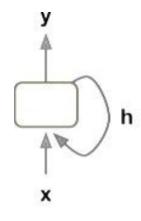
RNN: Optimization

Backward Propagation through Time

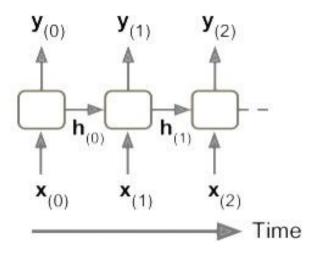


How to Addressing Vanishing Gradient?

Dominant approach: Use Long Short Term Memory Networks (LSTM)

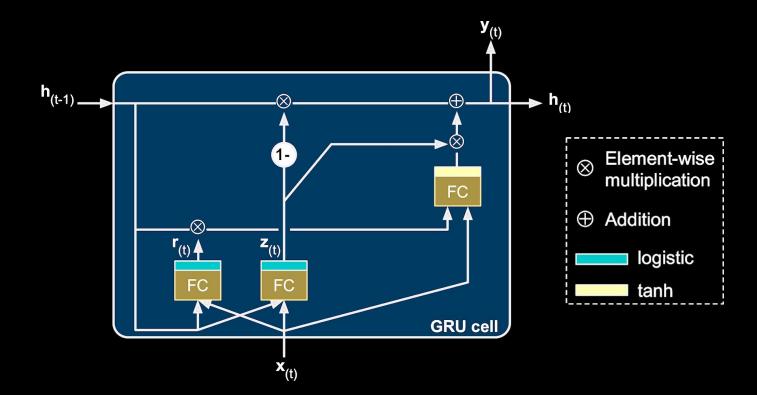


RNN model

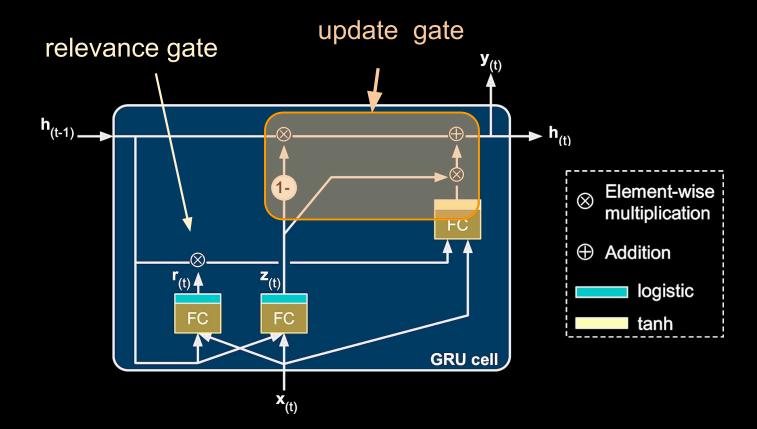


"unrolled" depiction

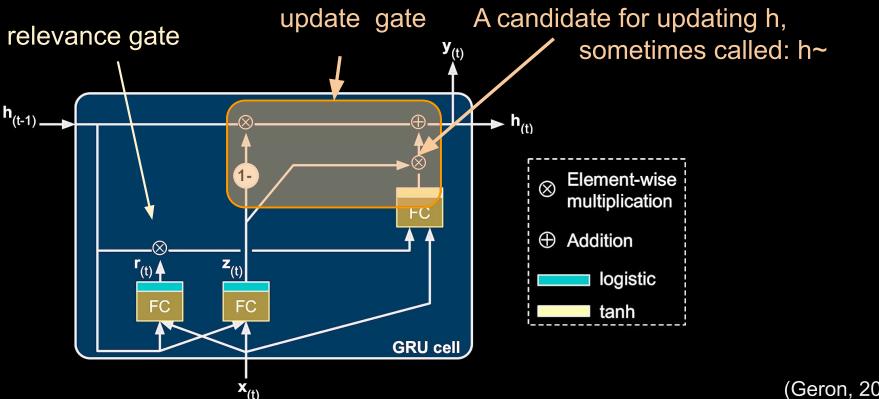
Gated Recurrent Unit



Gated Recurrent Unit



Gated Recurrent Unit



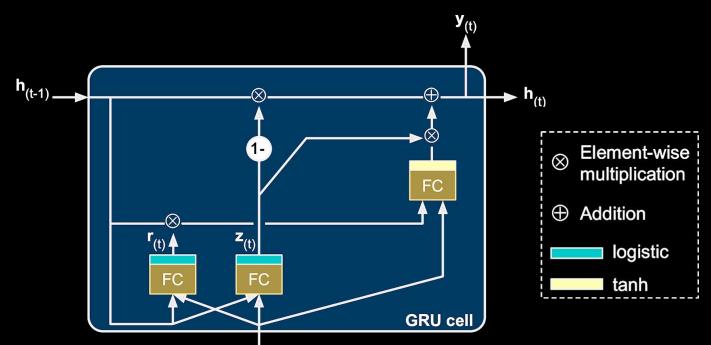
Gated Recurrent Unit

$$\mathbf{z}_{(t)} = \sigma(\mathbf{W}_{xz}^{T} \cdot \mathbf{x}_{(t)} + \mathbf{W}_{hz}^{T} \cdot \mathbf{h}_{(t-1)} + \mathbf{b}_{z})$$

$$\mathbf{r}_{(t)} = \sigma(\mathbf{W}_{xr}^{T} \cdot \mathbf{x}_{(t)} + \mathbf{W}_{hr}^{T} \cdot \mathbf{h}_{(t-1)} + \mathbf{b}_{r})$$

$$\mathbf{g}_{(t)} = \tanh(\mathbf{W}_{xg}^{T} \cdot \mathbf{x}_{(t)} + \mathbf{W}_{hg}^{T} \cdot (\mathbf{r}_{(t)} \otimes \mathbf{h}_{(t-1)}) + \mathbf{b}_{g})$$

$$\mathbf{h}_{(t)} = \mathbf{z}_{(t)} \otimes \mathbf{h}_{(t-1)} + (1 - \mathbf{z}_{(t)}) \otimes \mathbf{g}_{(t)}$$



The cake, which contained candles, was eaten.

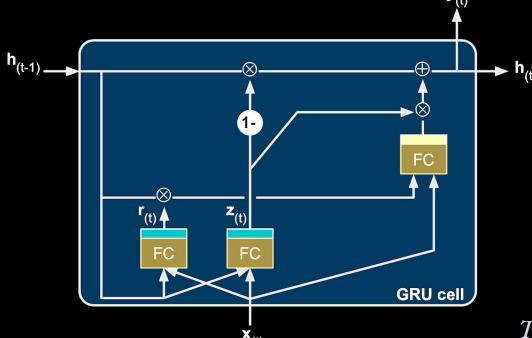
What about the gradient?

$$\mathbf{z}_{(t)} = \sigma(\mathbf{W}_{xz}^T \cdot \mathbf{x}_{(t)} + \mathbf{W}_{hz}^T \cdot \mathbf{h}_{(t-1)} + \mathbf{b}_z)$$

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$$\mathbf{h}_{(t)} = \mathbf{z}_{(t)} \otimes \mathbf{h}_{(t-1)} + (1 - \mathbf{z}_{(t)}) \otimes \mathbf{g}_{(t)}$$



The gates (i.e. multiplications based on a logistic) often end up keeping the hidden state exactly (or nearly exactly) as it was. Thus, for most dimensions of h,

$$h_{(t)} \approx h_{(t-1)}$$

The cake, which contained candles, was eaten.

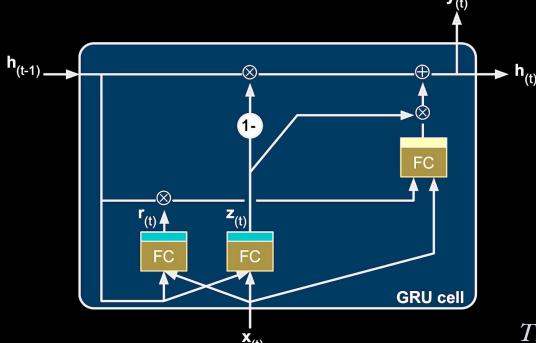
What about the gradient?

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$$\mathbf{h}_{(t)} = \mathbf{z}_{(t)} \otimes \mathbf{h}_{(t-1)} + (1 - \mathbf{z}_{(t)}) \otimes \mathbf{g}_{(t)}$$



The gates (i.e. multiplications based on a logistic) often end up keeping the hidden state exactly (or nearly exactly) as it was. Thus, for most dimensions of h,

$$h_{(t)} \approx h_{(t-1)}$$

This tends to keep the gradient from vanishing since the same values will be present through multiple times in backpropagation through time. (The same idea applies to LSTMs but is easier to see here).

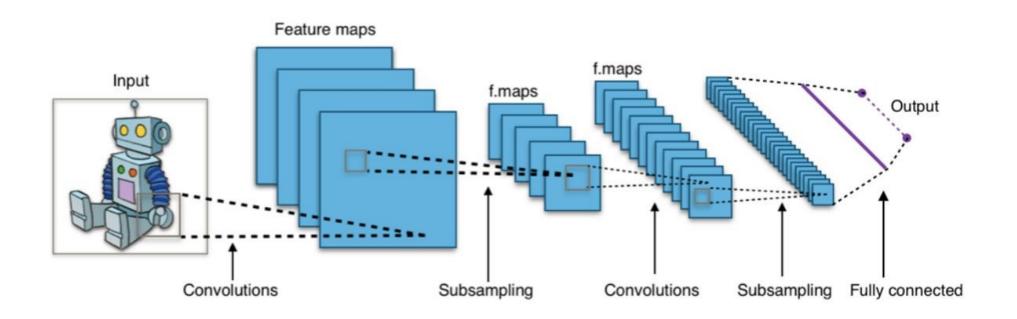
The cake, which contained candles, was eaten.

The GRU (LSTM): Zoomed out

Take-Aways

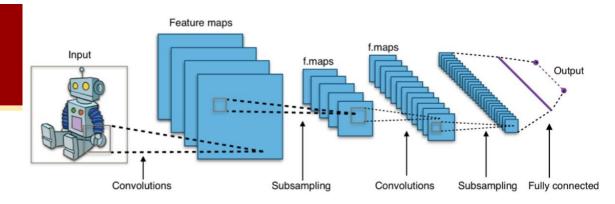
- Simple RNNs are powerful models but they are difficult to train:
 - O Just two functions $h_{(t)}$ and $y_{(t)}$ where $h_{(t)}$ is a combination of $h_{(t-1)}$ and $x_{(t)}$.
 - Exploding and vanishing gradients make training difficult to converge.
- LSTM (e.g. GRU cells) solve
 - Hidden states pass from one time-step to the next, allow for long-distance dependencies.
 - Gates are used to keep hidden states from changing rapidly (and thus keeps gradients under control).
 - To train: mini-batch stochastic gradient descent over cross-entropy cost^{tion}

Convolutional Neural Networks



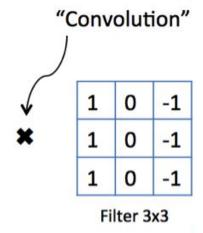
(wikipedia)

Convolution Layer



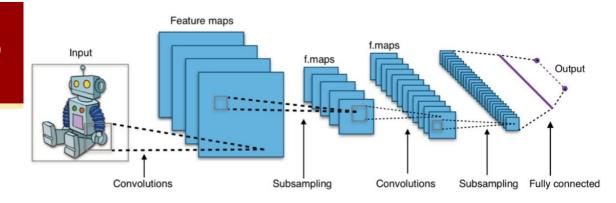
3	1	1	2	8	4
1	0	7	3	2	6
2	3	5	1	1	3
1	4	1	2	6	5
3	2	1	3	7	2
9	2	6	2	5	1

Original image 6x6



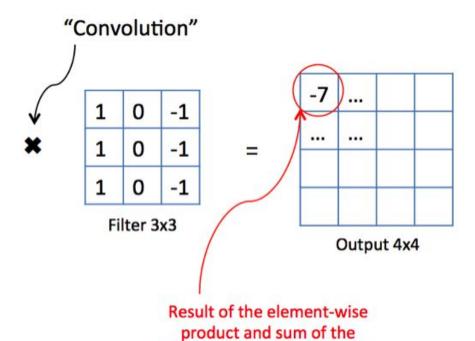
(Barter, 2018)

Convolution Layer



3	1	1	2	8	4
1	0	7	3	2	6
2	3	5	1	1	3
1	4	1	2	6	5
3	2	1	3	7	2
9	2	6	2	5	1

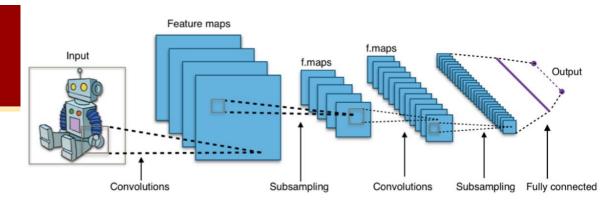
Original image 6x6



filter matrix and the <u>orginal</u> image

(Barter, 2018)

Convolution Layer



3	1	1	2	8	4
1	0	7	3	2	6
2	3	5	1	1	3
1	4	1	2	6	5
3	2	1	3	7	2
9	2	6	2	5	1

Original image 6x6

"Convolution"

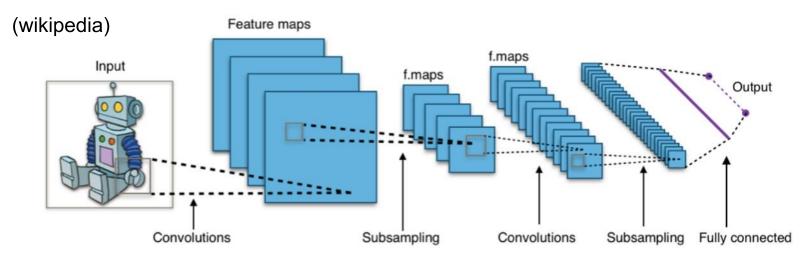
1 0 -1
1 0 -1
1 0 -1
Filter 3x3

Output 4x4

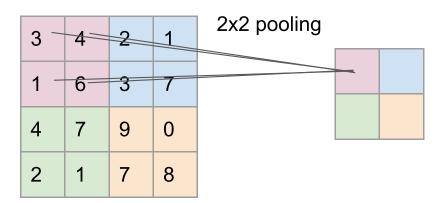
Breakthrough in image classification: Let the model automatically learn the filter weights!

Result of the element-wise product and sum of the filter matrix and the <u>orginal</u> image

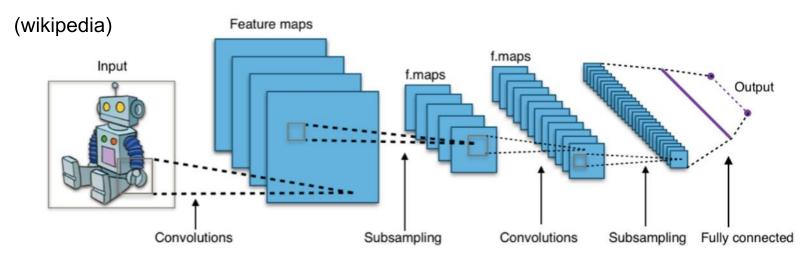
Subsampling (Pooling)



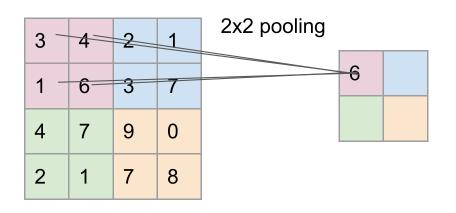
Subsampling -- reducing total grid size (i.e. reducing parameters for next layer)



Subsampling (Pooling)



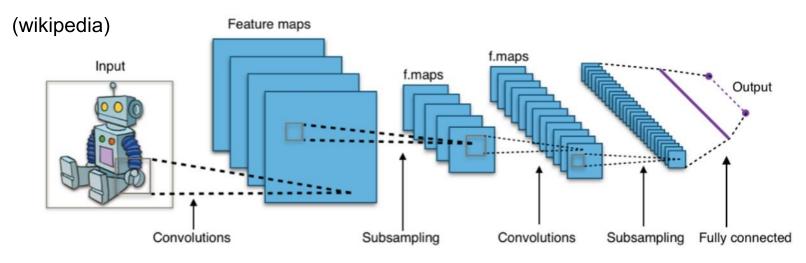
Subsampling -- reducing total grid size (i.e. reducing parameters for next layer)



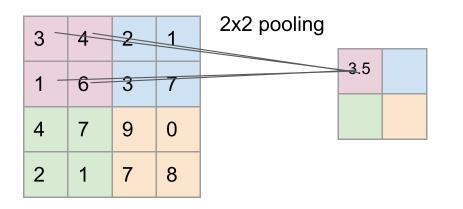
Types of pooling

- max
- avg

Subsampling (Pooling)



Subsampling -- reducing total grid size (i.e. reducing parameters for next layer)



Types of pooling

- max
- avg

Standard Training Loss Function

Logistic Regression Likelihood:
$$L(\beta_0, \beta_1, ..., \beta_k | X, Y) = \prod_{i=1}^n p(x_i)^{y_i} (1 - p(x_i))^{1-y_i}$$

Final Cost Function:
$$J^{(t)} = -\frac{1}{N}\sum_{i=1}^N\sum_{j=1}^{|V|}y_{i,j}^{(t)}\log~\hat{y}_{i,j}^{(t)}$$
 -- "cross entropy error"

Standard Training Loss Function

RNN cost = tf.reduce mean(-tf.reduce sum(y*tf.log(y pred)) #where did this come from?

Logistic Regression Likelihood: $L(\beta_0,\beta_1,...,\beta_k|X,Y) = \prod_{i=1}^n p(x_i)^{y_i}(1-p(x_i))^{1-y_i}$ Log Likelihood: $\ell(\beta) = \sum_{i=1}^N y_i log \ p(x_i) + (1-y_i) log \ (1-p(x_i))$ Log Loss: $J(\beta) = -\frac{1}{N} \sum_{i=1}^N y_i log \ p(x_i) + (1-y_i) log \ (1-p)(x_i))$

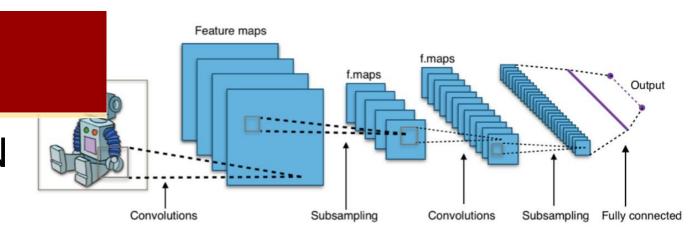
 $J = -\frac{1}{N} \sum_{i=1}^{N} \sum_{j=1}^{|V|} y_i log \ p(x_{i,j}) \qquad \text{(a "multiclass" log loss)}$ **Cross-Entropy Cost:**

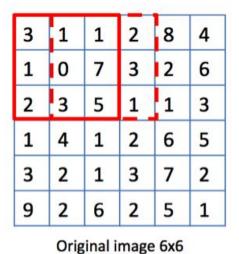
Final Cost Function: $J^{(t)} = -\frac{1}{N}\sum_{i=1}^N\sum_{j=1}^{|V|}y_{i,j}^{(t)}\log~\hat{y}_{i,j}^{(t)}$ -- "cross entropy error"

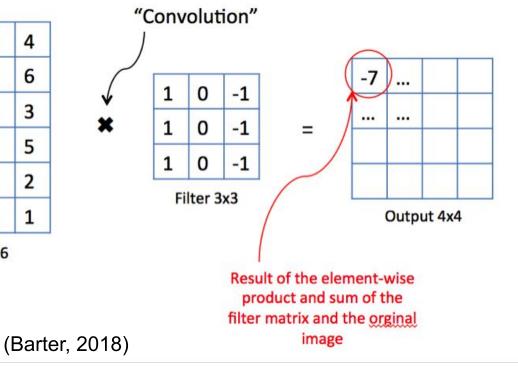
Review Net input Activation Inputs Weights function function Feed Forward Network (full-connected) (skymind, Al Wiki) output layer input layer hidden layer 1 hidden layer 2

Review

Convolutional NN







Review

Recurrent Neural Network

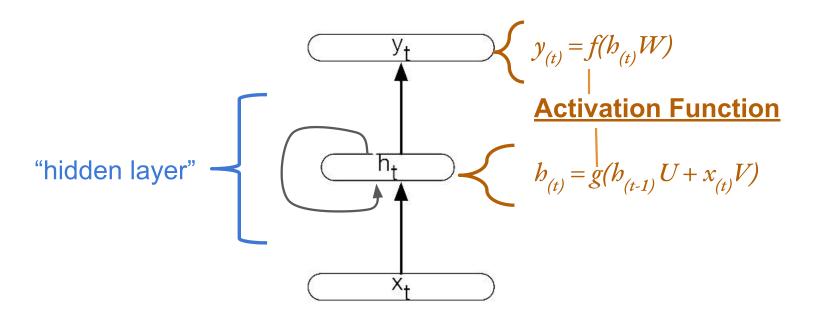
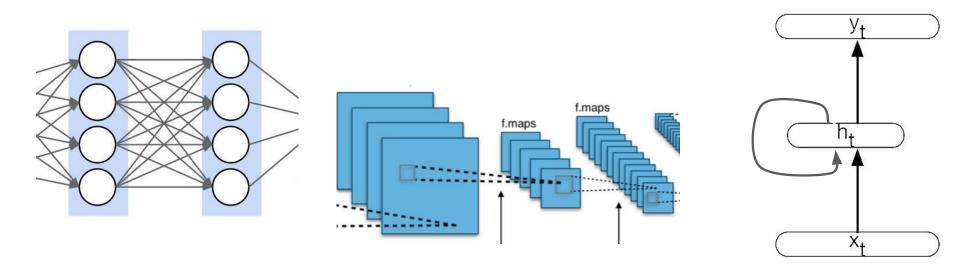


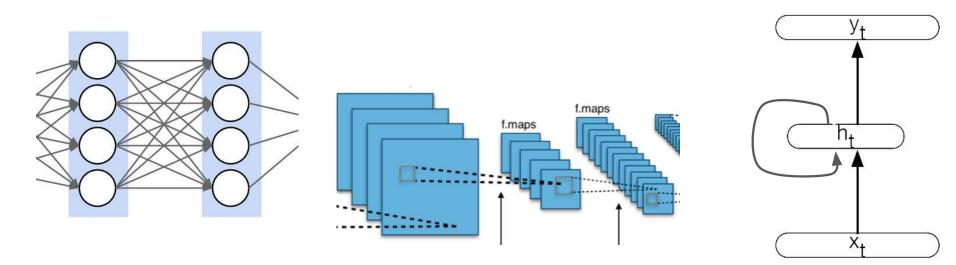
Figure 9.2 Simple recurrent neural network after Elman (Elman, 1990). The hidden layer includes a recurrent connection as part of its input. That is, the activation value of the hidden layer depends on the current input as well as the activation value of the hidden layer from the previous timestep.

(Jurafsky, 2019)



Can model computation (e.g. matrix operations for a single input) be parallelized?

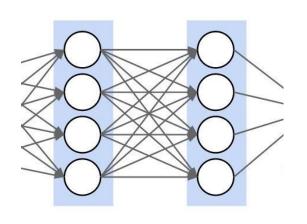


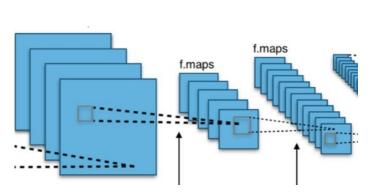


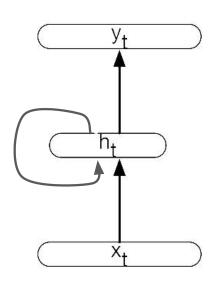
Can model computation (e.g. matrix operations for a single input) be parallelized?









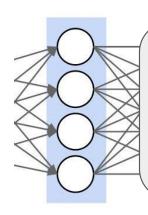


Can model computation (e.g. matrix operations for a single input) be parallelized?

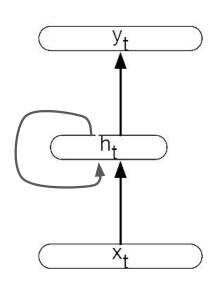








Ultimately limits how complex the model can be (i.e. it's total number of paramers/weights) as compared to a CNN.



Can model computation (e.g. matrix operations for a singra









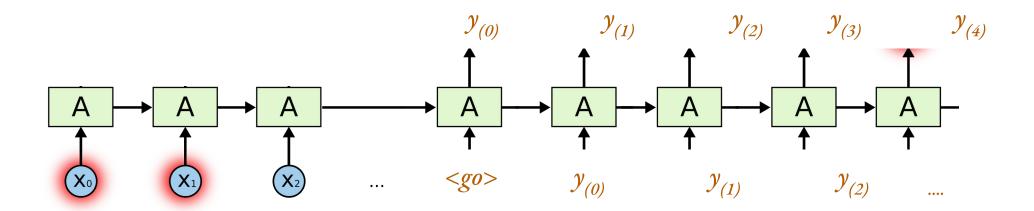
Can handle sequences and long-distance dependencies, but....

- Don't want complexity of LSTM/GRU cells
- Constant num edges between input steps
- Enables "interactions" (i.e. adaptations) between words
- Easy to parallelize -- don't need sequential processing.

Challenge:

The ball was kicked by kayla.

Long distance dependency when translating:

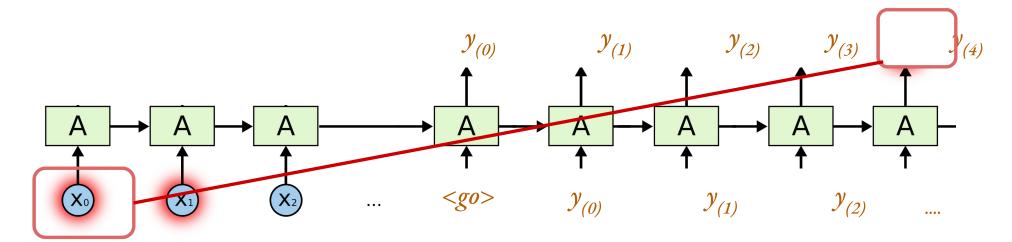


Kayla kicked the ball.

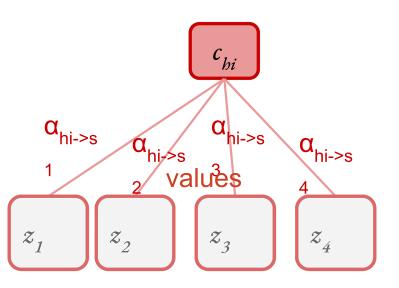
Challenge:

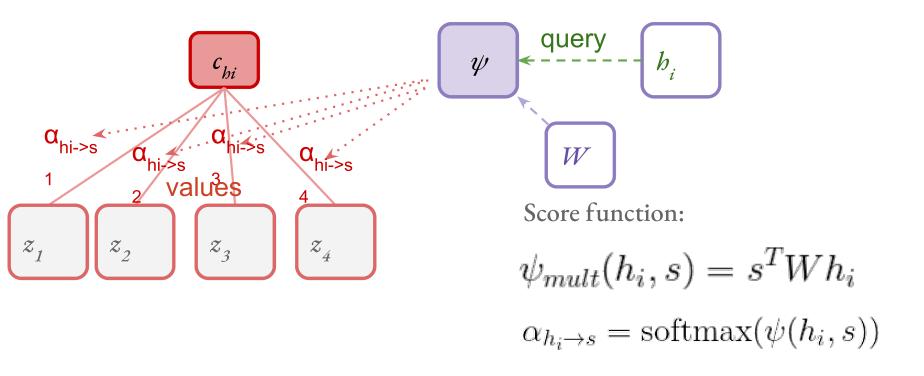
The ball was kicked by kayla.

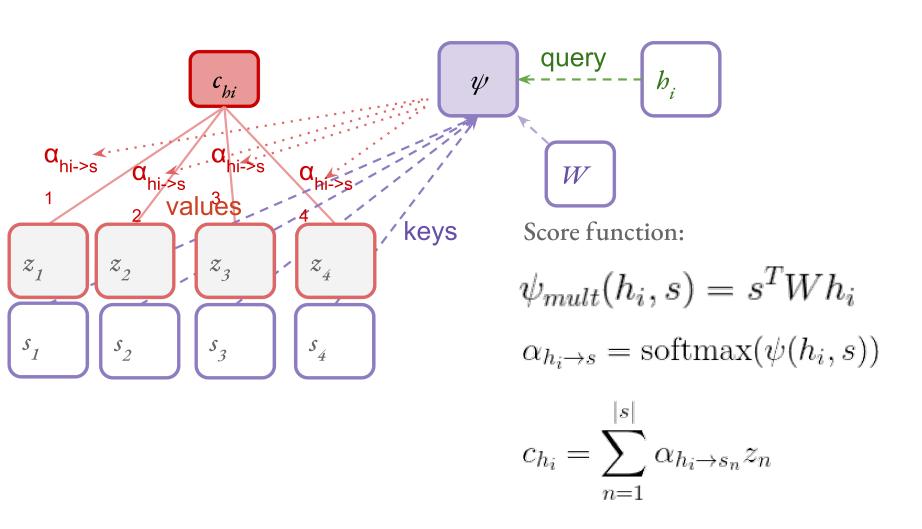
Long distance dependency when translating:



Kayla kicked the ball.







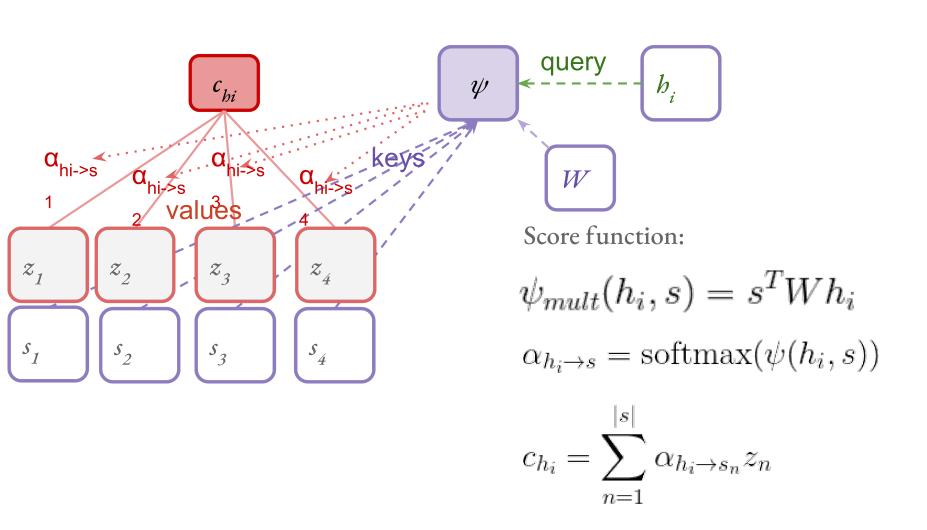
ttion only modele

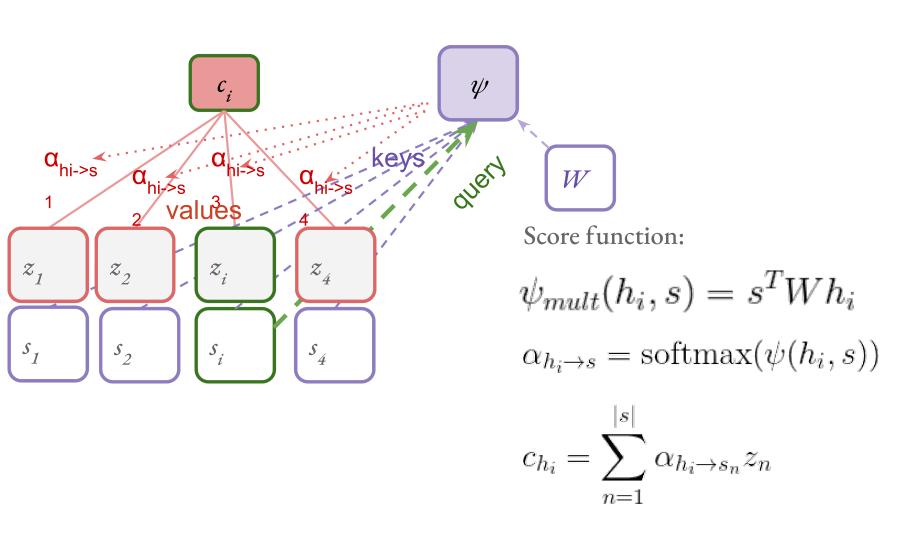
Challenge:

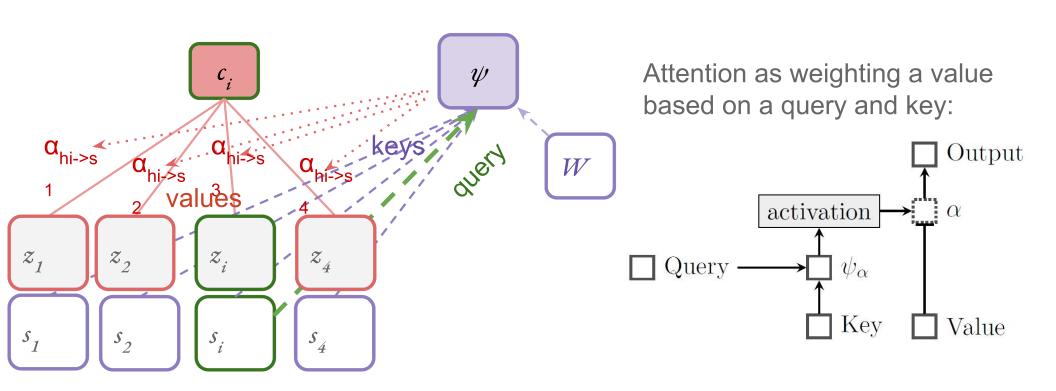
Long distance dependency when translating:

Attention came about for encoder decoder models.

Then self-attention was introduced:

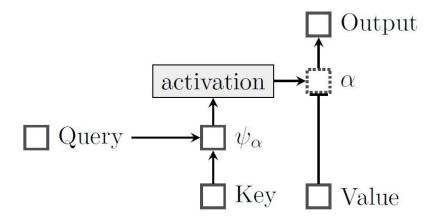


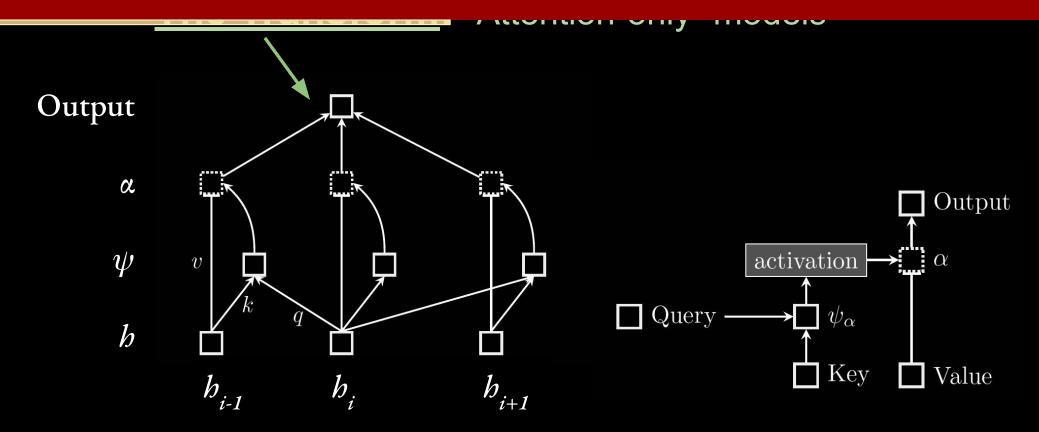


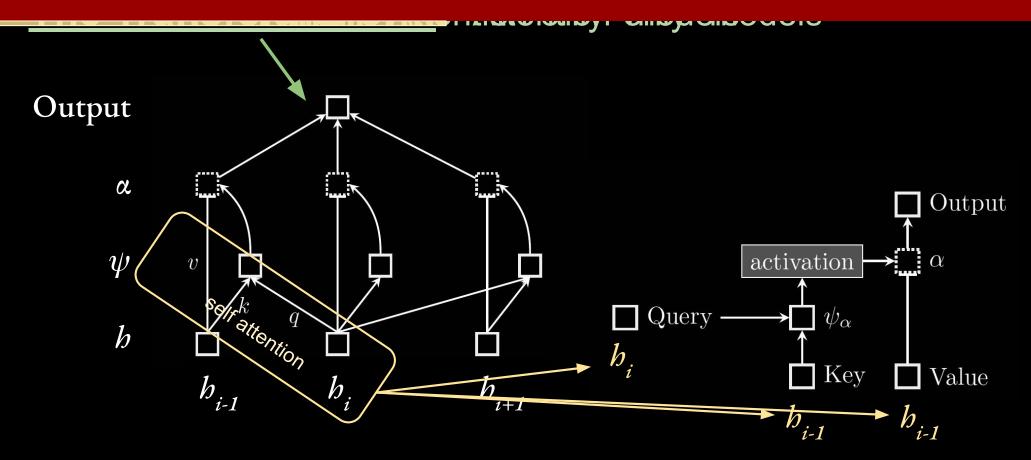


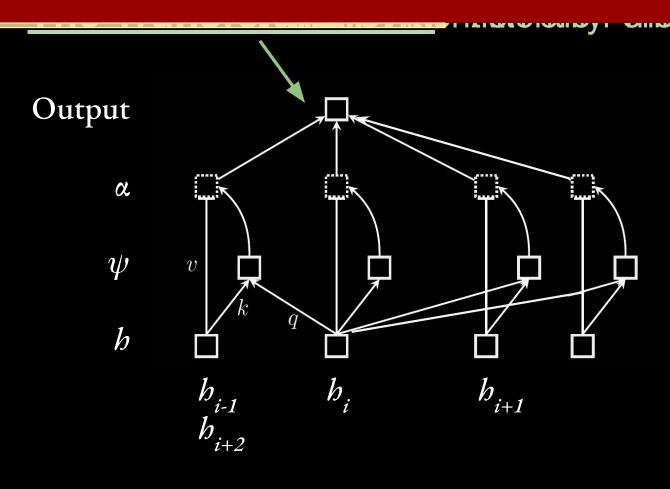
THEORET OF THOUSE

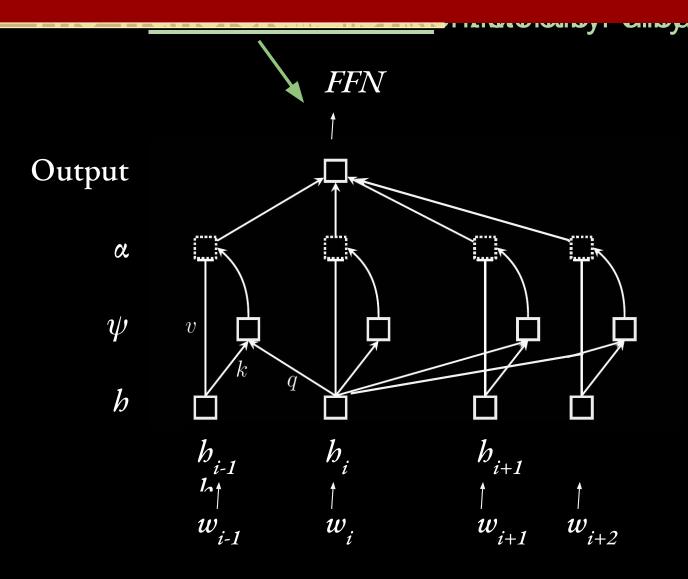
Attention as weighting a value based on a query and key:

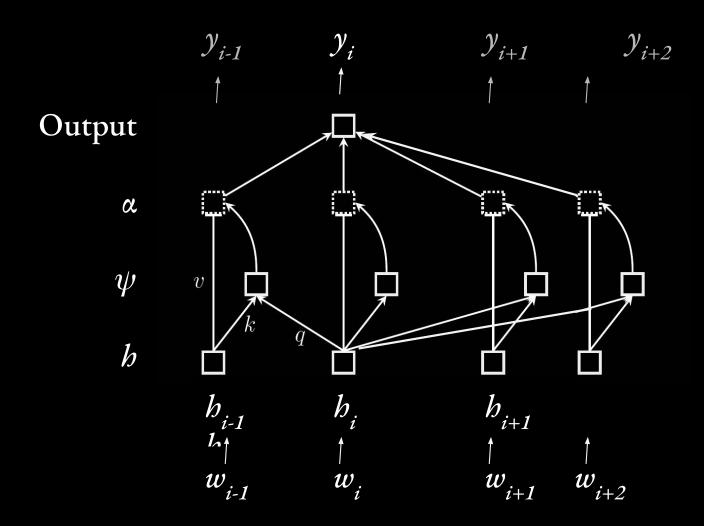


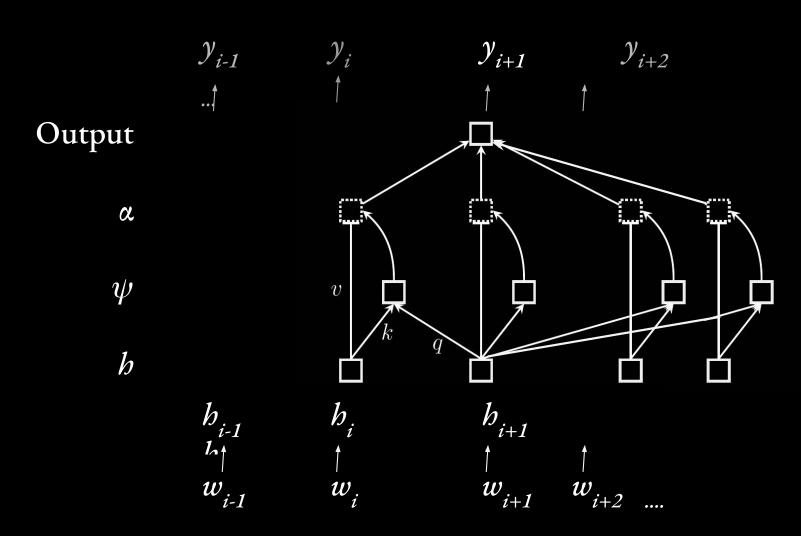


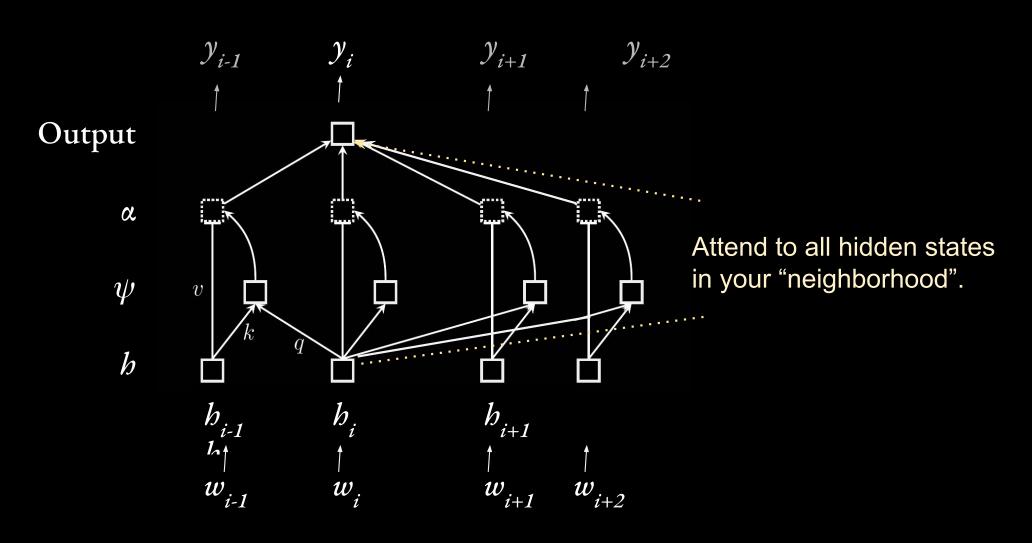


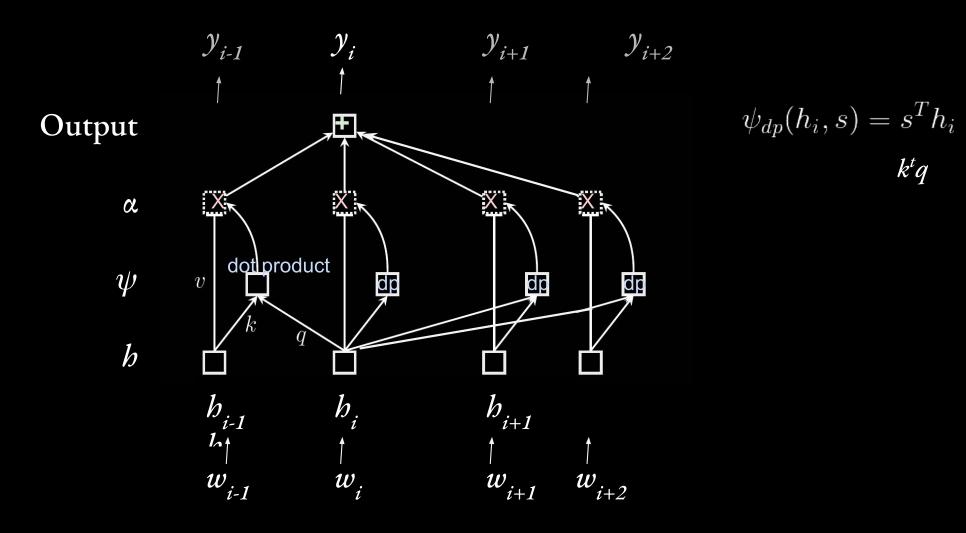


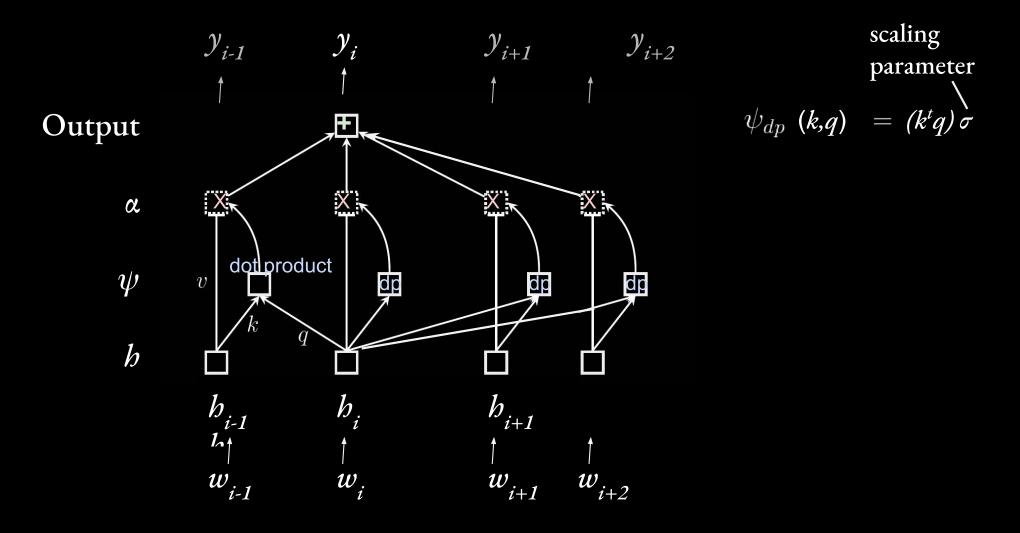


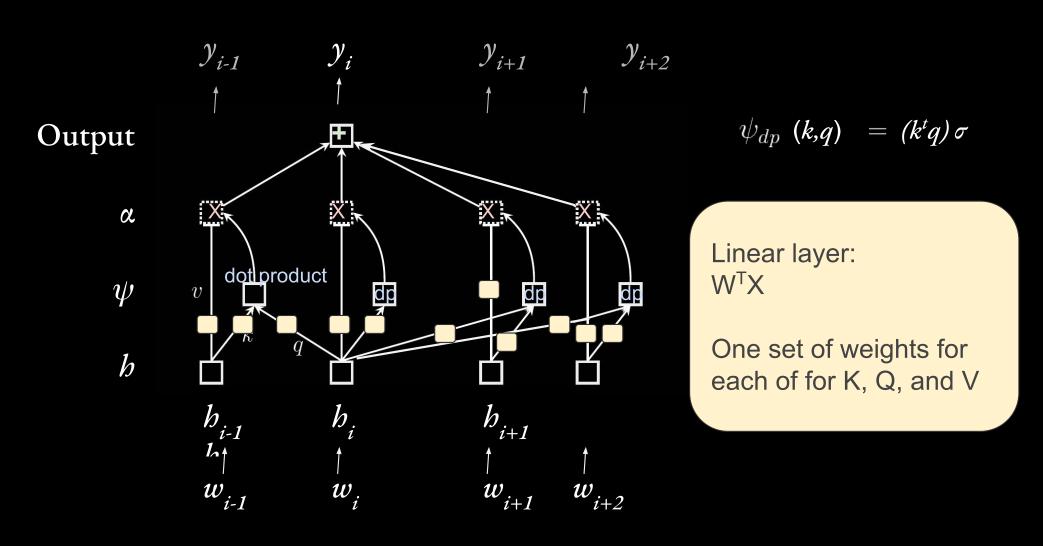






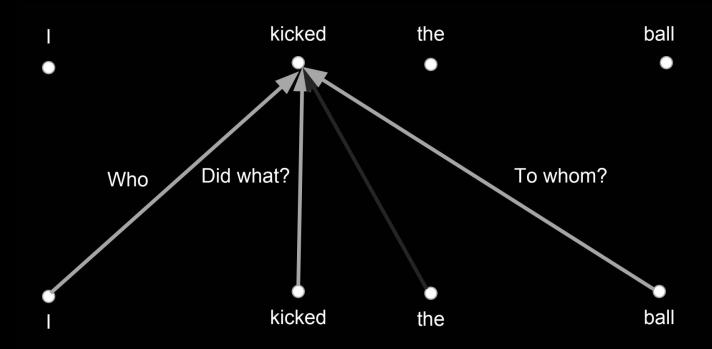






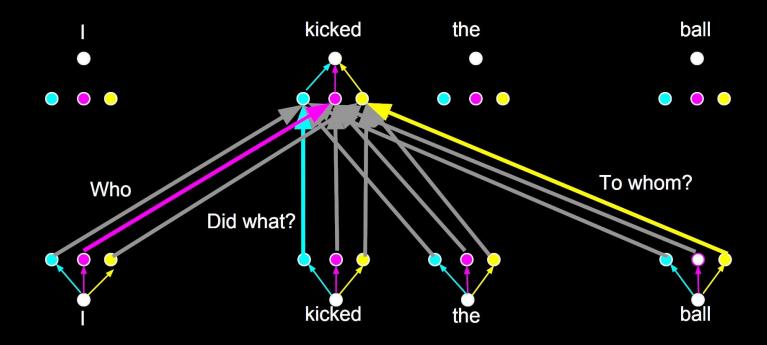
The Transformer

Limitation (thus far): Can't capture multiple types of dependencies between words.

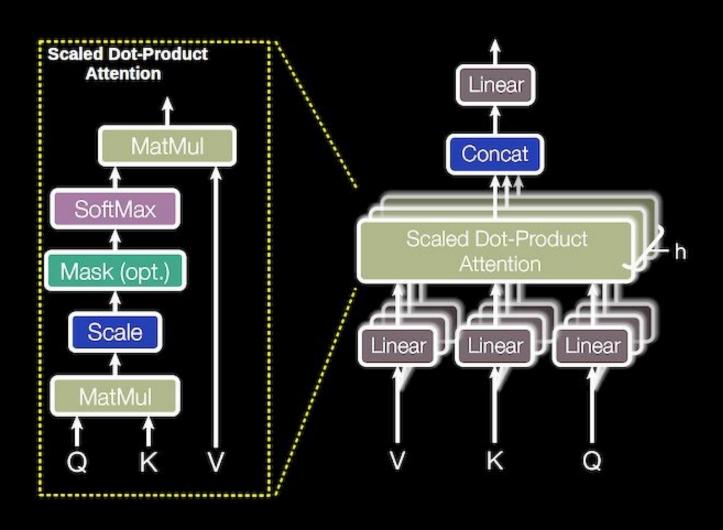


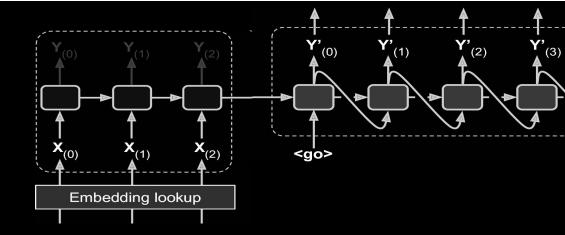
The Transformer

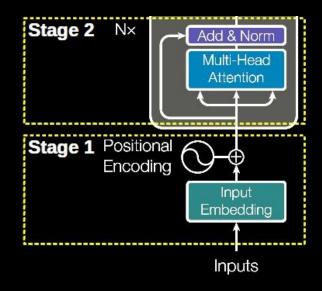
Solution: Multi-head attention



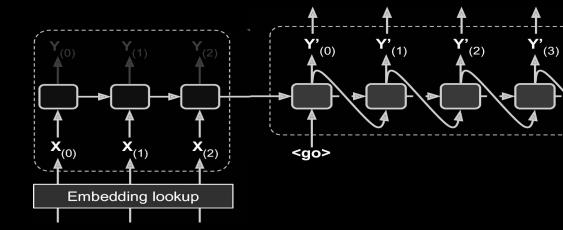
Multi-head Attention

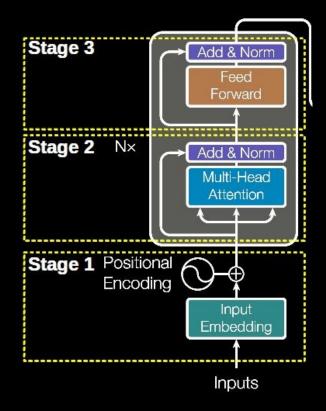


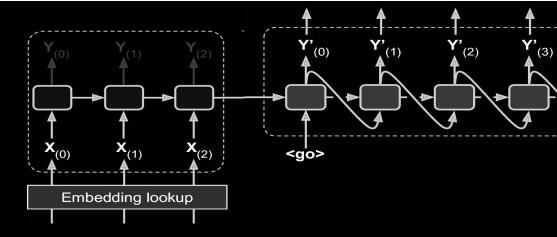


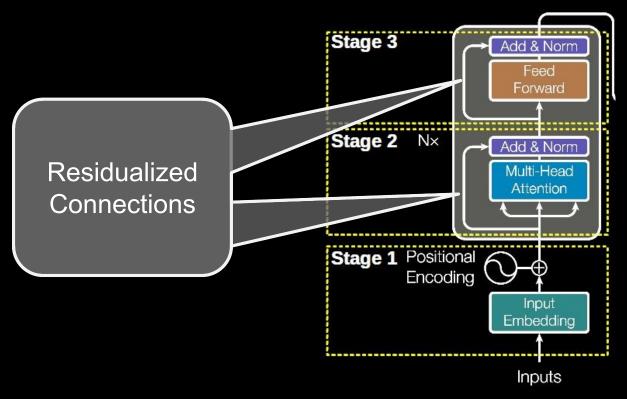


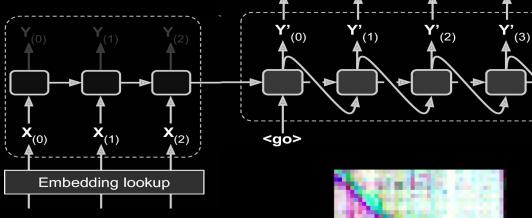
(3) **Transformer for Encoder-Decoder** <g'o> Embedding lookup sequence index (t) Stage 2 Add & Norm Multi-Head Attention Stage 1 Positional **POSITIONAL** 0.84 0.0001 0.54 Input **ENCODING Embedding EMBEDDINGS** Inputs INPUT

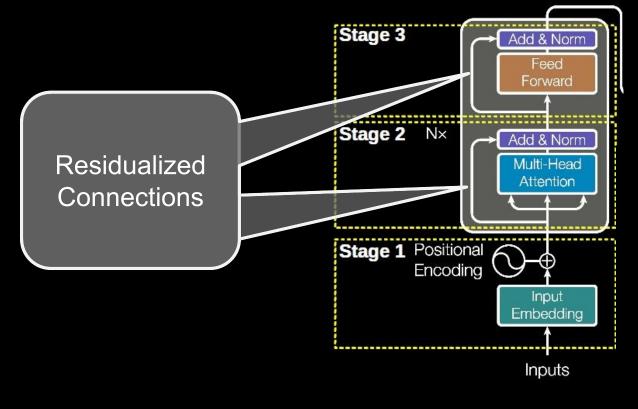








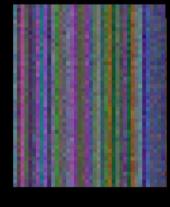




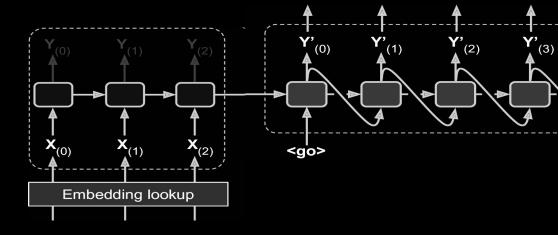
residuals enable positional information to be passed along

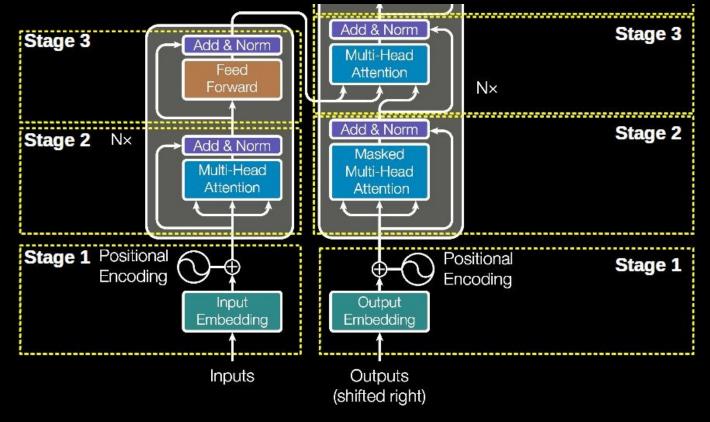


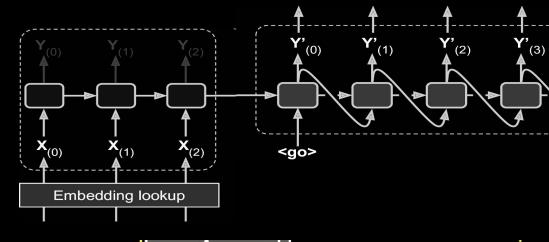
With residuals



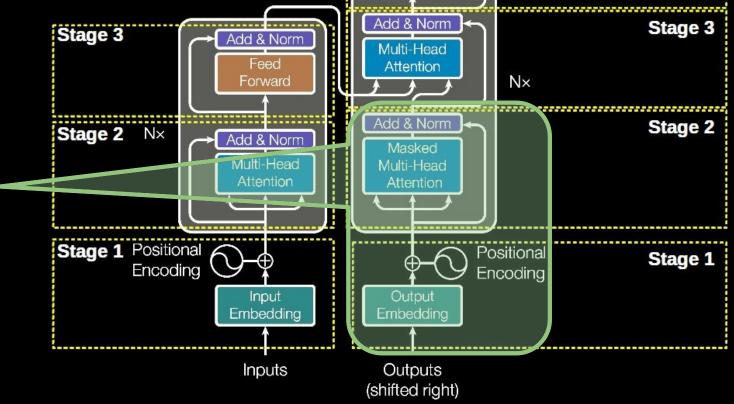
Without residuals



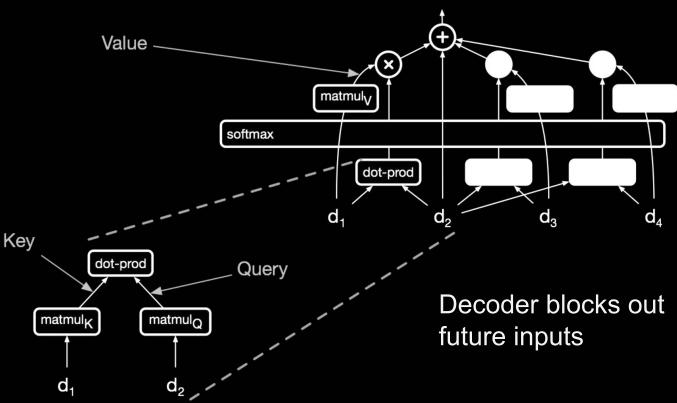


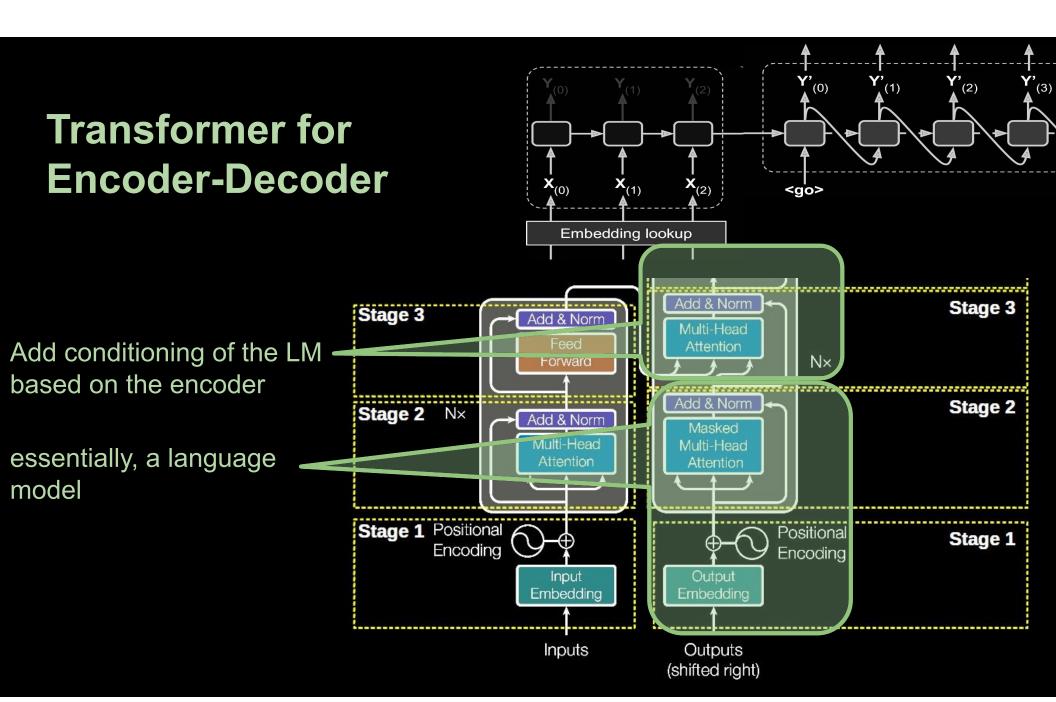


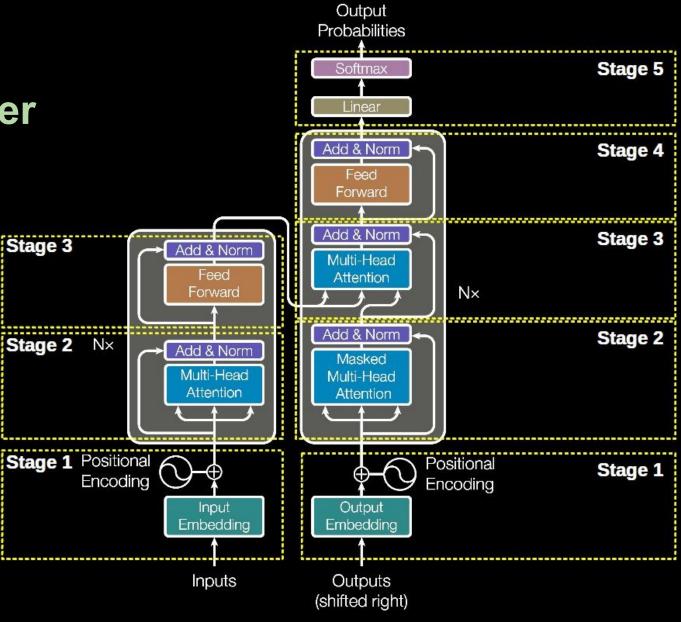
essentially, a language model



essentially, a language model







Transformer (as of 2017)

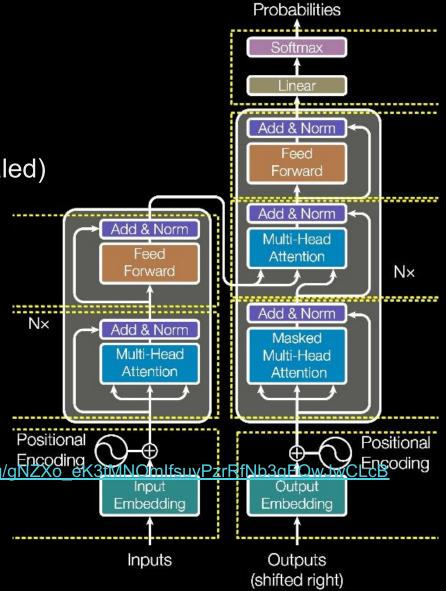
"WMT-2014" Data Set. BLEU scores:

	EN-DE	EN-FR
GNMT (orig)	24.6	39.9
ConvSeq2Seq	25.2	40.5
Transformer*	28.4	41.8

Transformer

- Utilize Self-Attention
- Simple att scoring function (dot product, scaled)
- Added linear layers for Q, K, and V
- Multi-head attention
- Added positional encoding
- Added residual connection
- Simulate decoding by masking

Positional https://4.bp.blogspot.com/-OlrV-PAtEkQ/W3RkOJCBkal/AAAAAAAAADOg/gNZXo_erGAs/s640/image1.gif



Output

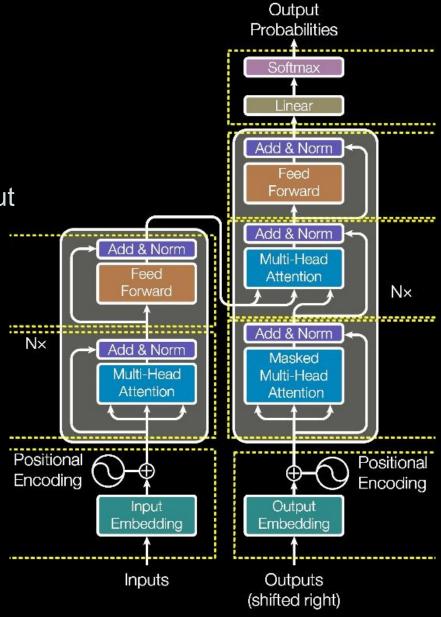
Transformer

Why?

- Don't need complexity of LSTM/GRU cells
- Constant num edges between words (or input steps)
- Enables "interactions" (i.e. adaptations) between words
- Easy to parallelize -- don't need sequential processing.

Drawbacks:

- Only unidirectional by default
- Only a "single-hop" relationship per layer (multiple layers to capture multiple)



BERT

Bidirectional Encoder Representations from Transformers

Produces contextualized embeddings (or pre-trained contextualized encoder)

Drawbacks of Vanilla Transformers:

- Only unidirectional by default
- Only a "single-hop" relationship per layer (multiple layers to capture multiple)

BERT

Bidirectional Encoder Representations from Transformers

Produces contextualized embeddings (or pre-trained contextualized encoder)

- Bidirectional context by "masking" in the middle
- A lot of layers, hidden states, attention heads.

Drawbacks of Vanilla Transformers:

- Only unidirectional by default
- Only a "single-hop" relationship per layer (multiple layers to capture multiple)

BERT

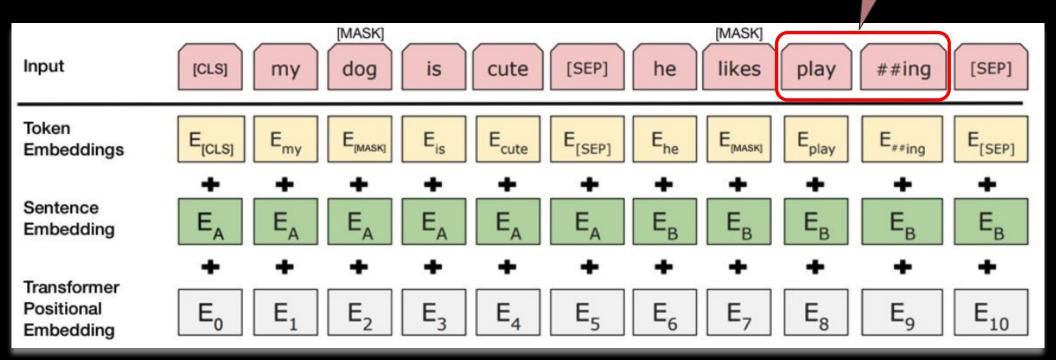
tokenize into "word pieces"

Sentence A = The man went to the store.

Sentence B = He bought a gallon of milk.

Label = IsNextSentence

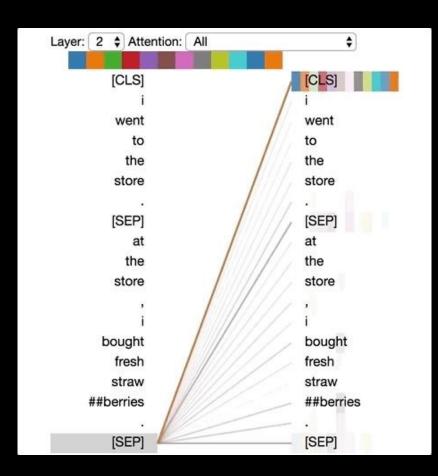
Sentence A = The man went to the store.
Sentence B = Penguins are flightless.
Label = NotNextSentence



(Devlin et al., 2019)

Bert: Attention by Layers

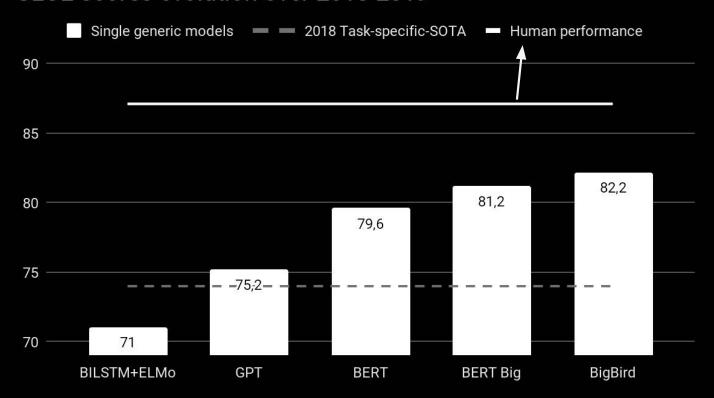
https://colab.research.google.com/drive/1vIOJ1lhdujVjfH857hvYKIdKPTD9Kid8



(Vig, 2019)

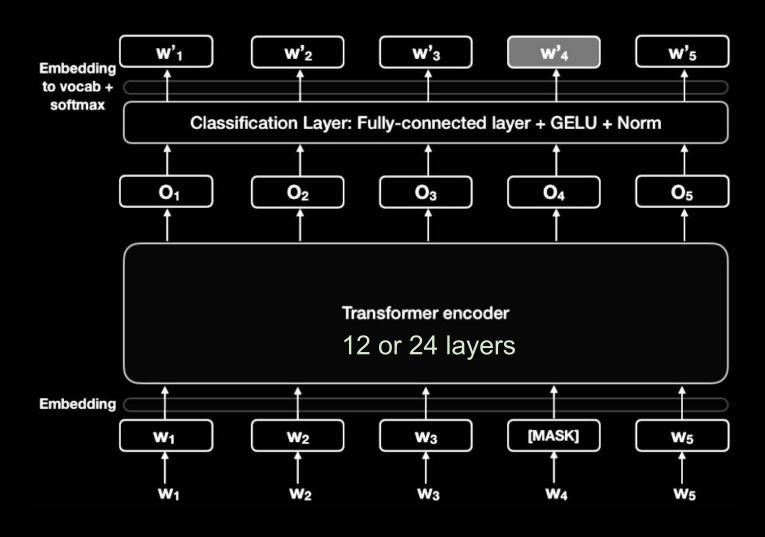
BERT Performance: e.g. Question Answering

GLUE scores evolution over 2018-2019

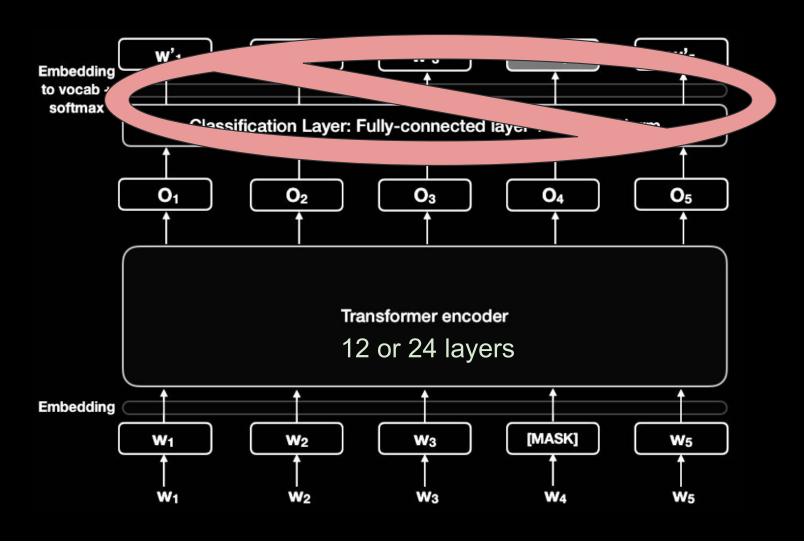


https://rajpurkar.github.io/SQuAD-explorer/

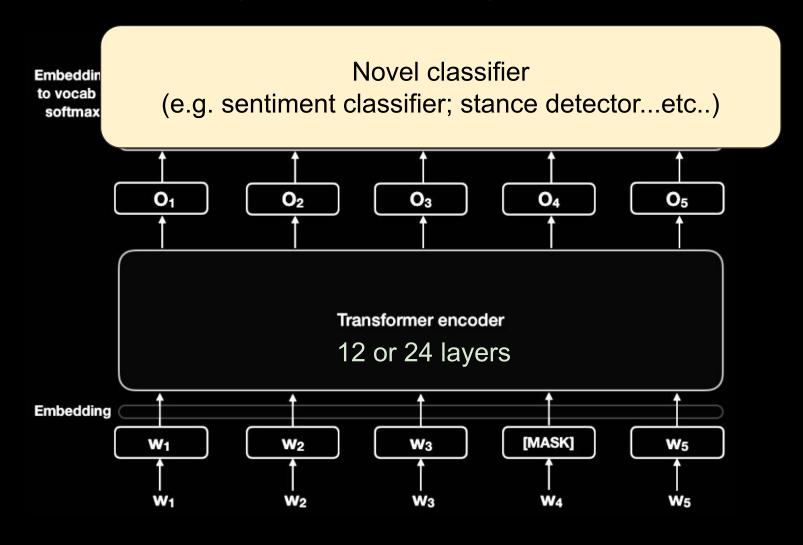
BERT: Pre-training; Fine-tuning



BERT: Pre-training; Fine-tuning



BERT: Pre-training; Fine-tuning



Summary

- Goal is accurate prediction of y (outcome) given features (x)
- Use L1 or L2 penalization (as a regularization) to avoid overfit
- Reason for Train, Dev, Test split
- Components of a neural network
- Batch Normalization
- Distribution options: why is data parallelism preferred?
- Recurrent Neural Network
- Convolution Operation with Filters